

Network Dynamics: Introduction

Introduction to Network Science

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Universitat
Pompeu Fabra
Barcelona

Content

- Introduction to network dynamics
- Spreading phenomena

Network dynamics

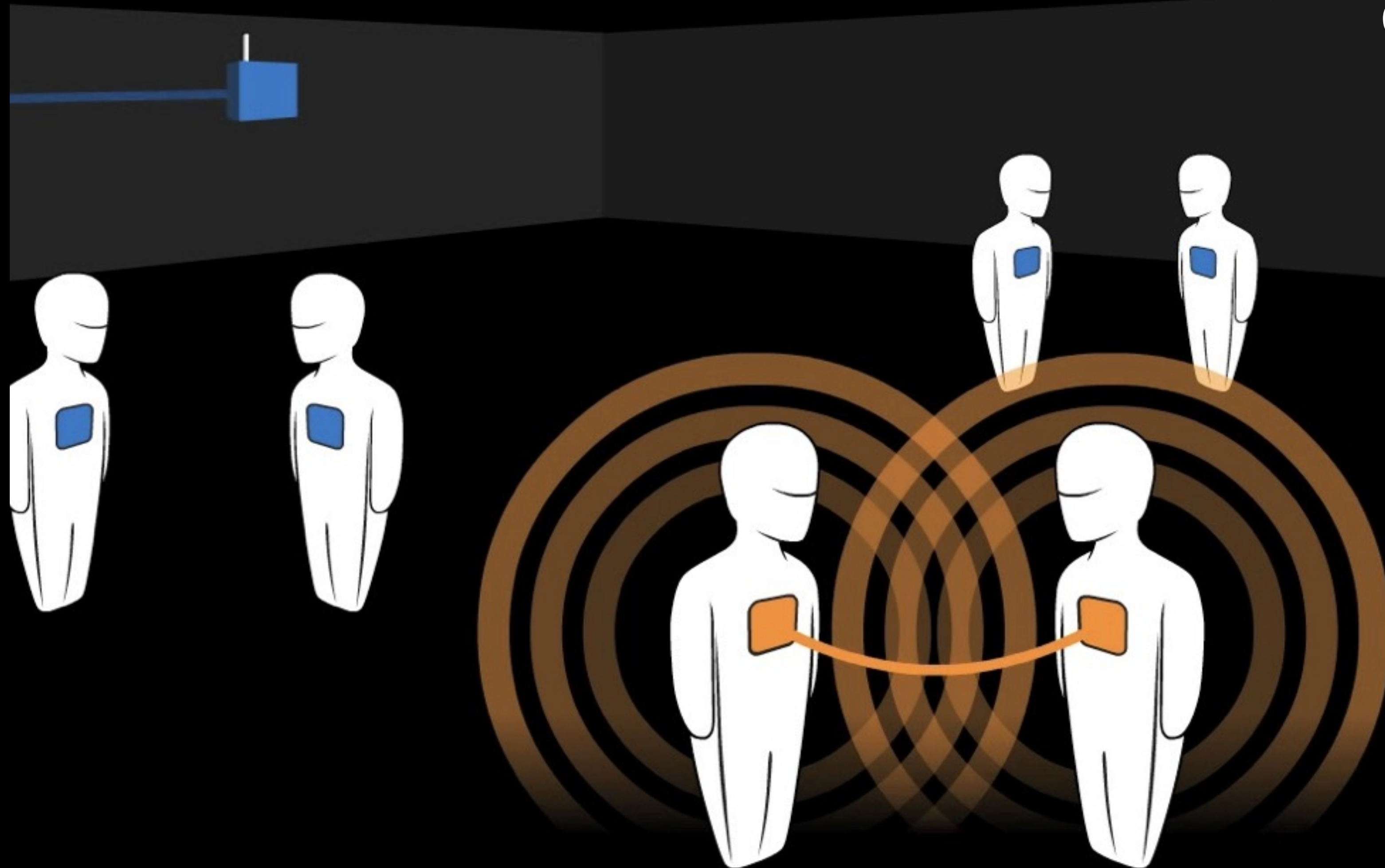
- Dynamics OF networks: time-evolving (temporal) networks
- Dynamics ON networks: stochastic processes on static networks
- Dynamics ON & OF networks: stochastic processes on temporal networks

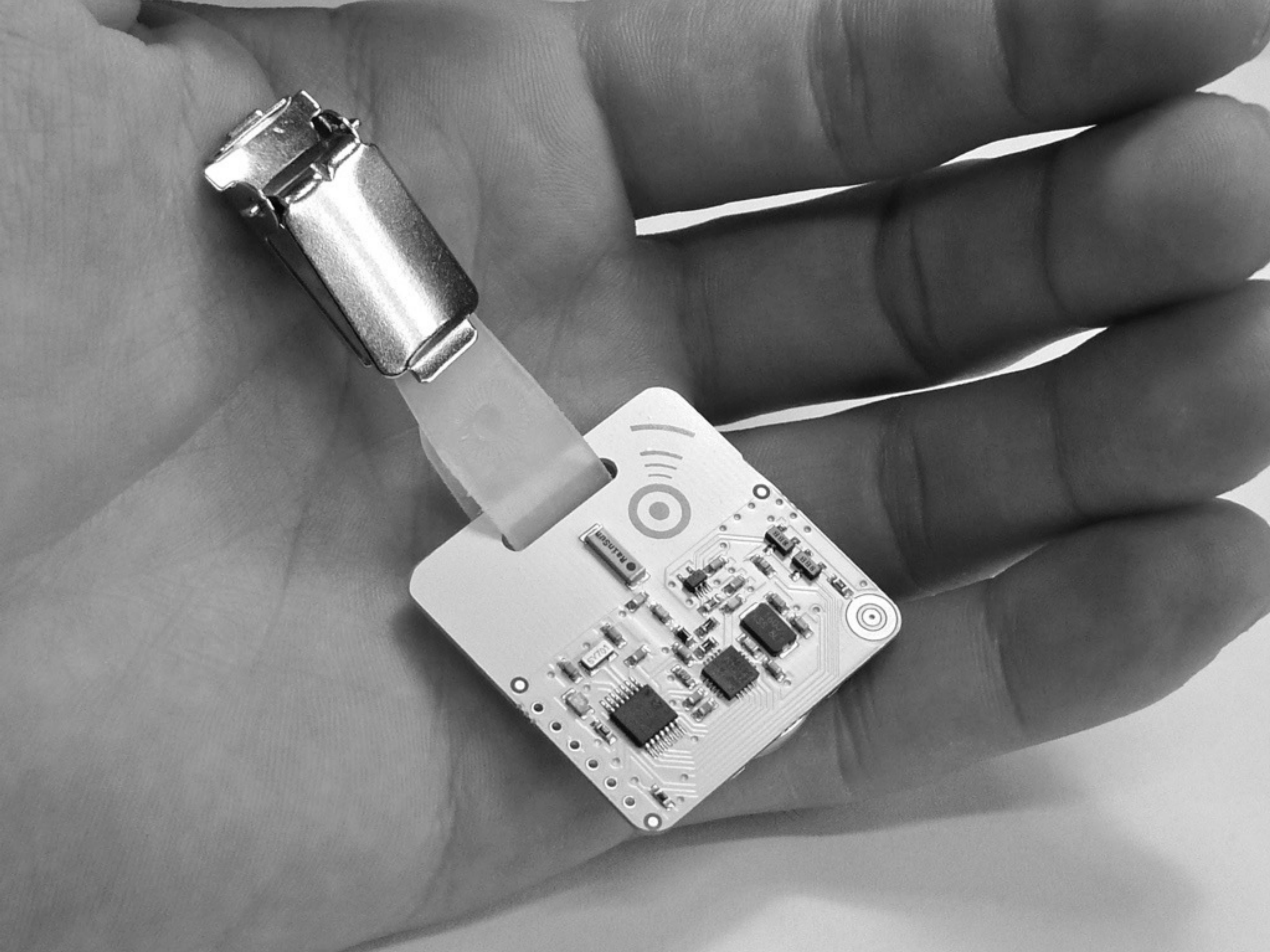
Temporal networks

- Temporal networks: links (and nodes) appear/disappear in time
- Online social networks: friendship created/removed, new users join/leave
- Contact networks: two persons interact for a while, then separate
- Communication network: each link (email) has instantaneous duration
- Transportation network: bus/train at a certain time
- Financial networks: financial transactions at a certain time

Face-to-face interaction networks

Conferences
Schools
Hospitals
Museums...



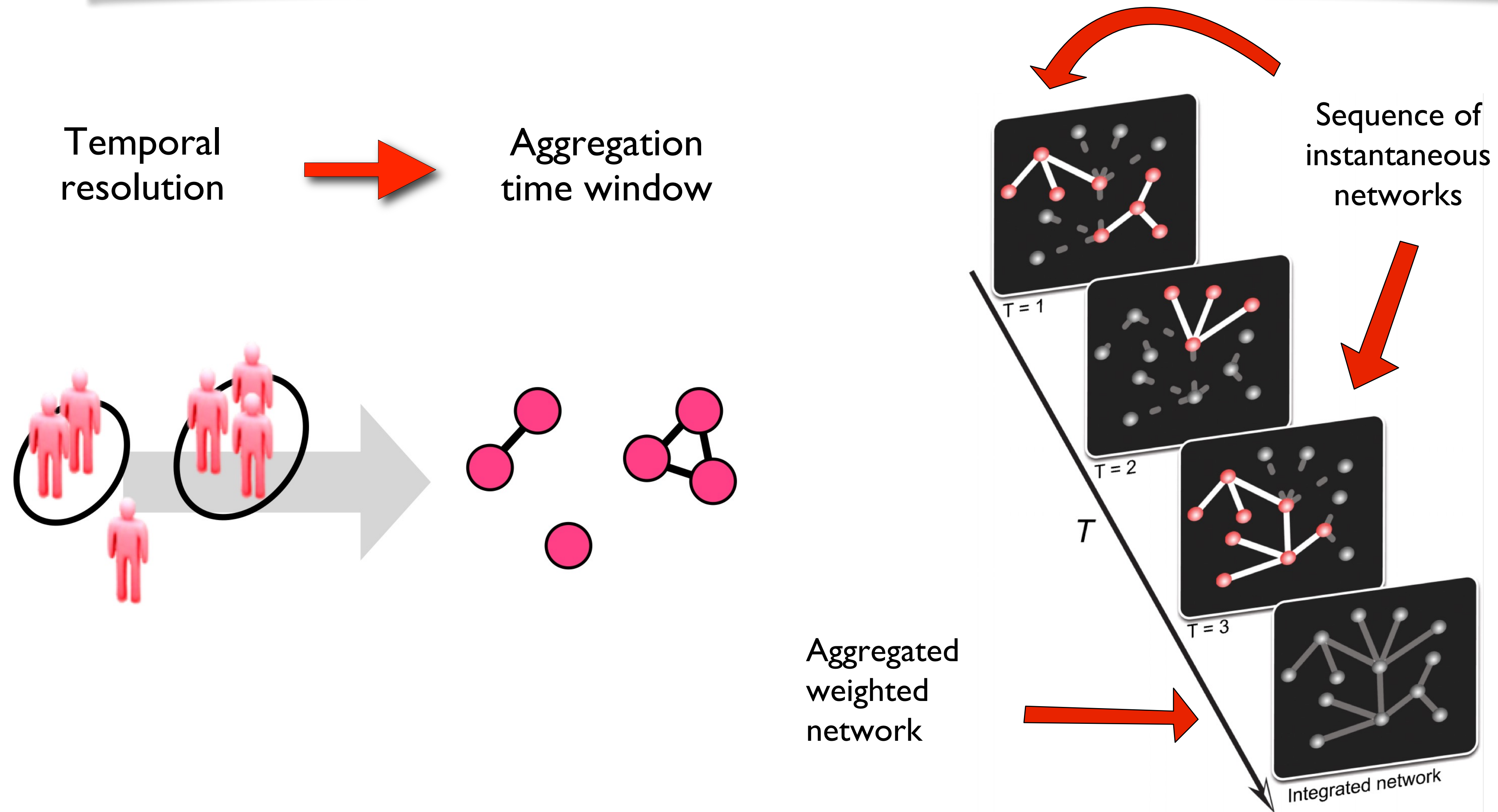


Temporal networks

1:00 - 2:30 PM

lunch, coffee and start of 3rd session

From f2f interactions to temporal networks



Dynamics on networks: Stochastic processes

- Information diffusion
- Epidemic spreading
- Opinion dynamics
- Synchronization

Stochastic processes on networks

- Each node i has a certain state x_i
- Such a state changes in time according to some rules, $x_i(t)$
- Random walk: $x_i=1$ if random walker is on node i , 0 otherwise
- Epidemics: $x_i=1$ if node i is infected, 0 otherwise
- Info diffusion: $x_i=1$ if node i knows a certain piece of info, 0 otherwise
- Opinion dynamics: $x_i=1$ if node holds opinion A (left), 0 otherwise (right)

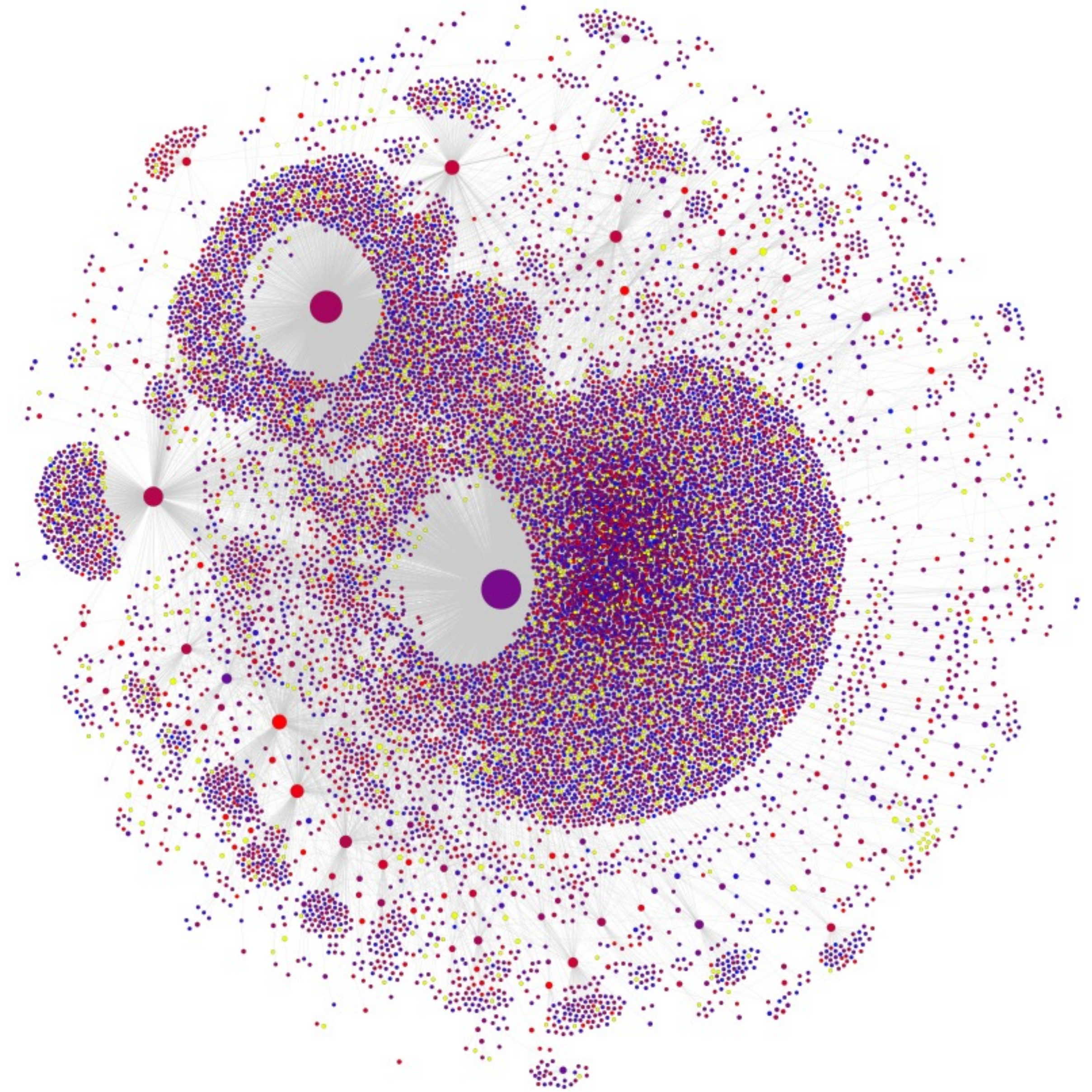
Stochastic processes on networks

- Each stochastic process is defined by the update rules
- How does state of node i changes in time, $x_i(t+1) = F(x_i(t), x_j(t), x_k(t), \dots)$?
- On networks, the state of node i only depends on the previous state of its neighbors: $x_i(t+1) = F(x_i(t), x_{j_1}(t), \dots, x_{j_k}(t), | j_1, \dots, j_k \text{ neighbors of node } i)$
- Random walk: $x_i(t+1) = 1$ if the RW was at some neighbour at time t
- Epidemics: $x_i(t+1) = 1$ (infected) if some neighbor was infected at time t
- Opinions: $x_i(t+1) = 1$ (opinion A) if the majority of neighbors hold opinion A

Spreading phenomena: fake news

A fake news article spreading
via Twitter during 2016 US
presidential campaign

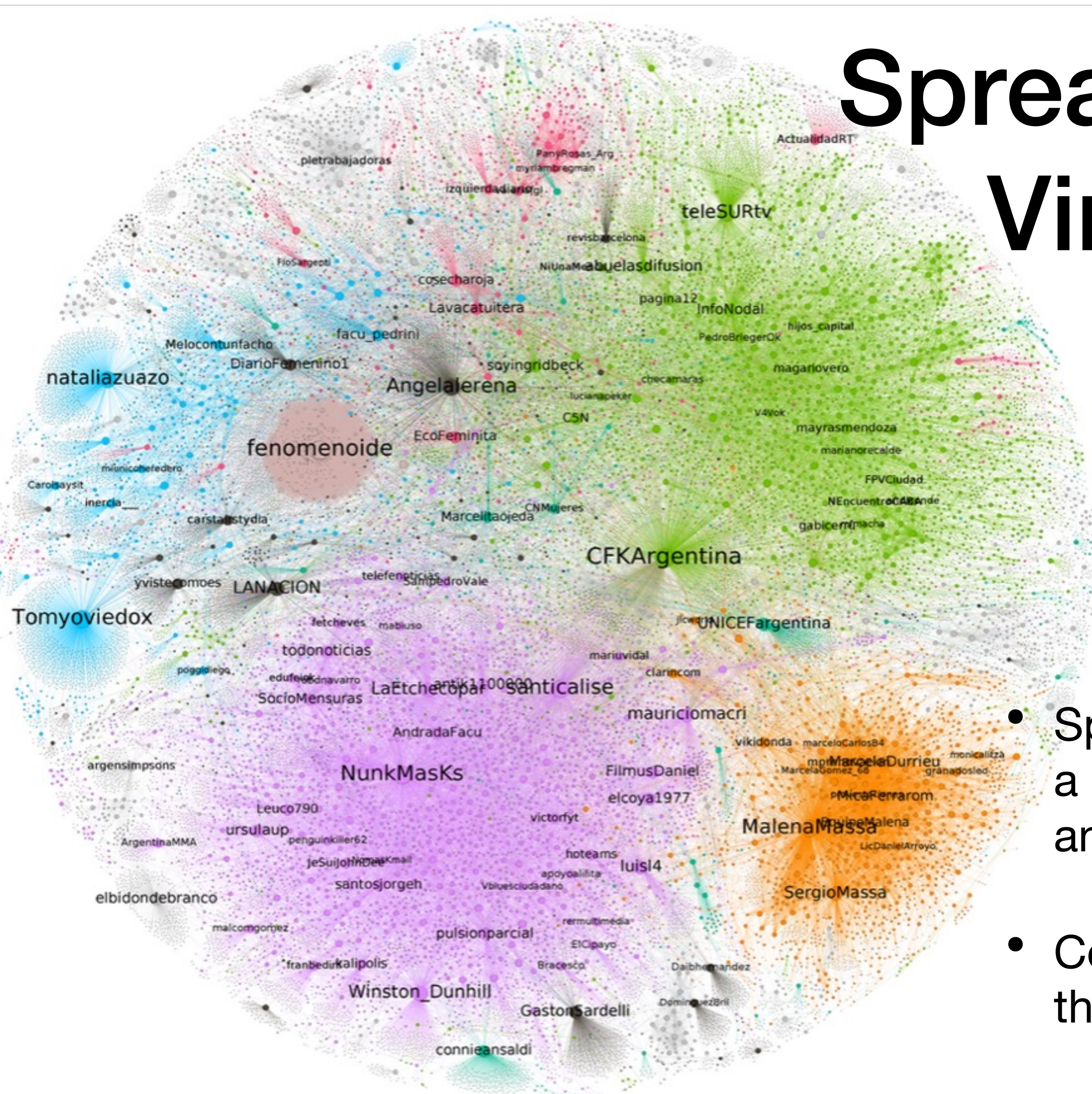
Red nodes are likely bots





“Influencers” and their sponsored posts

Spreading phenomena: Viral propagation



- Spread of the #NiUnaMenos hashtag: a movement against gender-based violence and femicide started in Argentina in 2015
- Colors based on communities detected through modularization optimization

Spreading phenomena: Non-trivial examples

- Back pain: spread from West to East in Germany after fall of Berlin Wall
- Suicide: well known to spread throughout communities on occasion
- Sexual “scripts”: expected sequences of behaviors during intimate situations
- Politics: the denser your connections, the more intense your convictions
- A wide array of phenomena spread through networks, not only viruses and information

Stochastic processes on temporal networks

- Both state of the nodes & presence/absence of links change in time
- The evolution of the process depends on the network dynamics

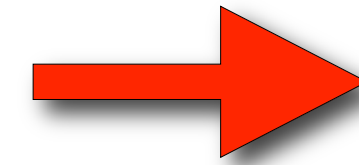
	Network	Process
Epidemic	Face-to-face contacts	Disease transmission
Information	Online social networks	News diffusion
Mobility	Transportation networks	Passengers flows

Stochastic processes on temporal networks

- The time scales of the network & process can be similar or very different
- Viral propagation on social media: viral propagation much faster (hours) than new connections on online social networks (weeks/months)
- Epidemic spreading: epidemic transmission (days) comparable with mobility (days)

Stochastic processes on temporal networks

- Process dynamics
- Time-varying network

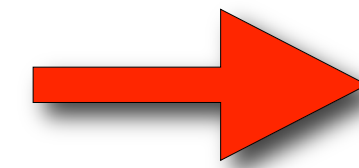


Time scales coupling

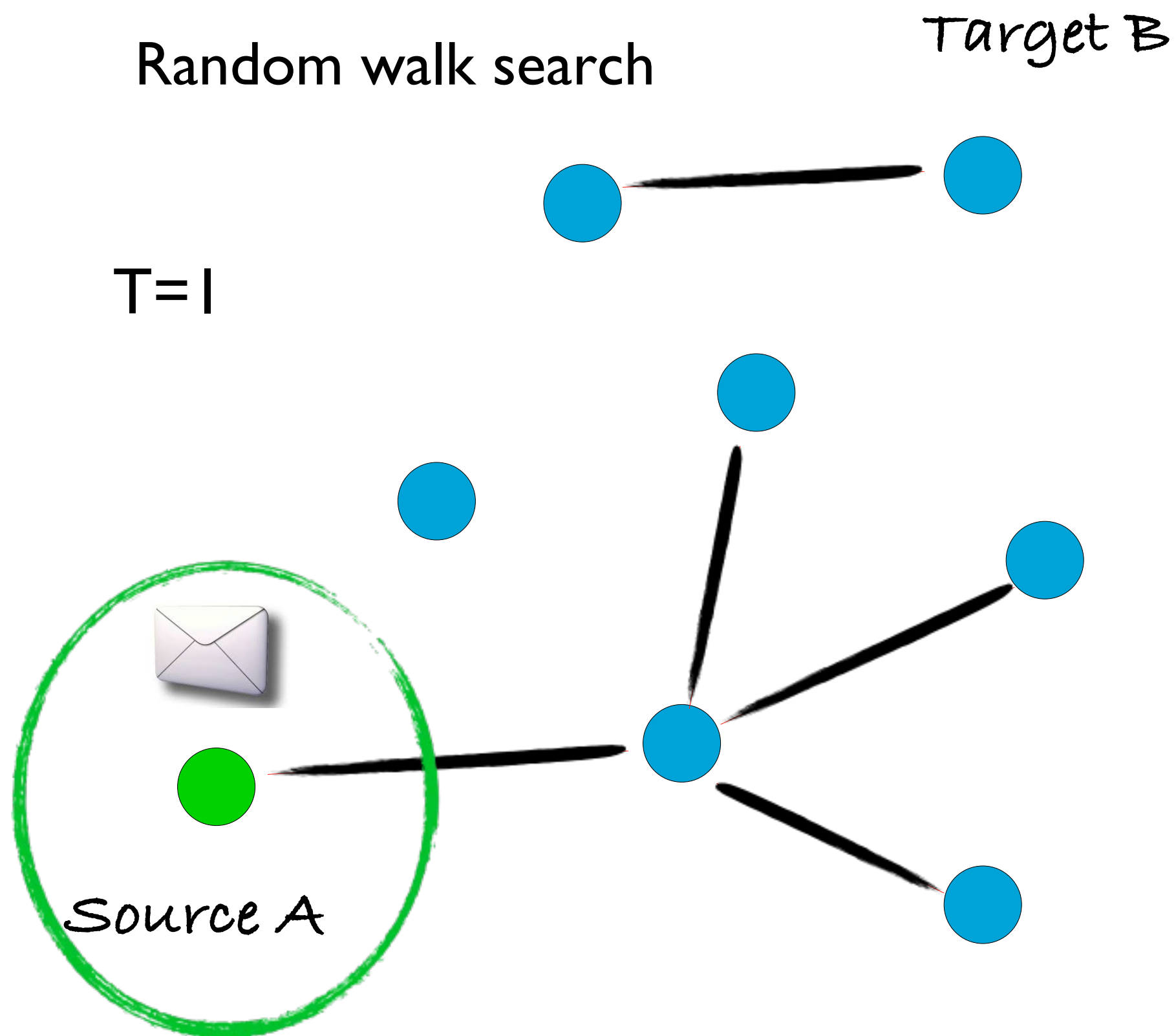
Random walk on a temporal network:
At each time step,
the letter takes one
available link at random

Dynamical processes on temporal networks

- Process dynamics
- Time-varying network



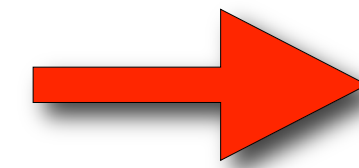
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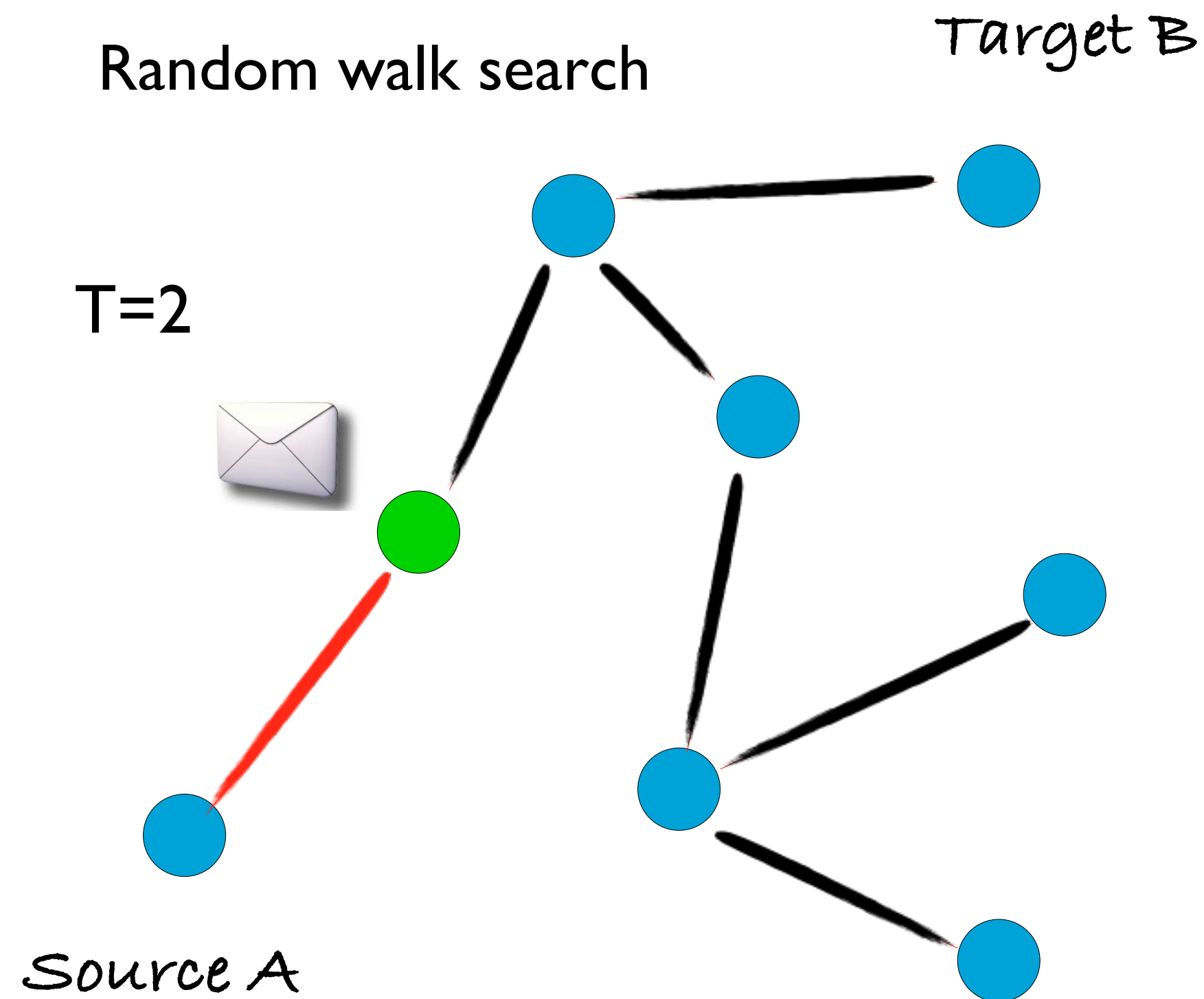
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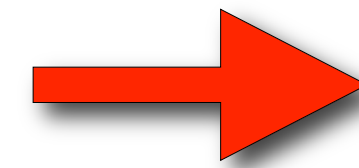
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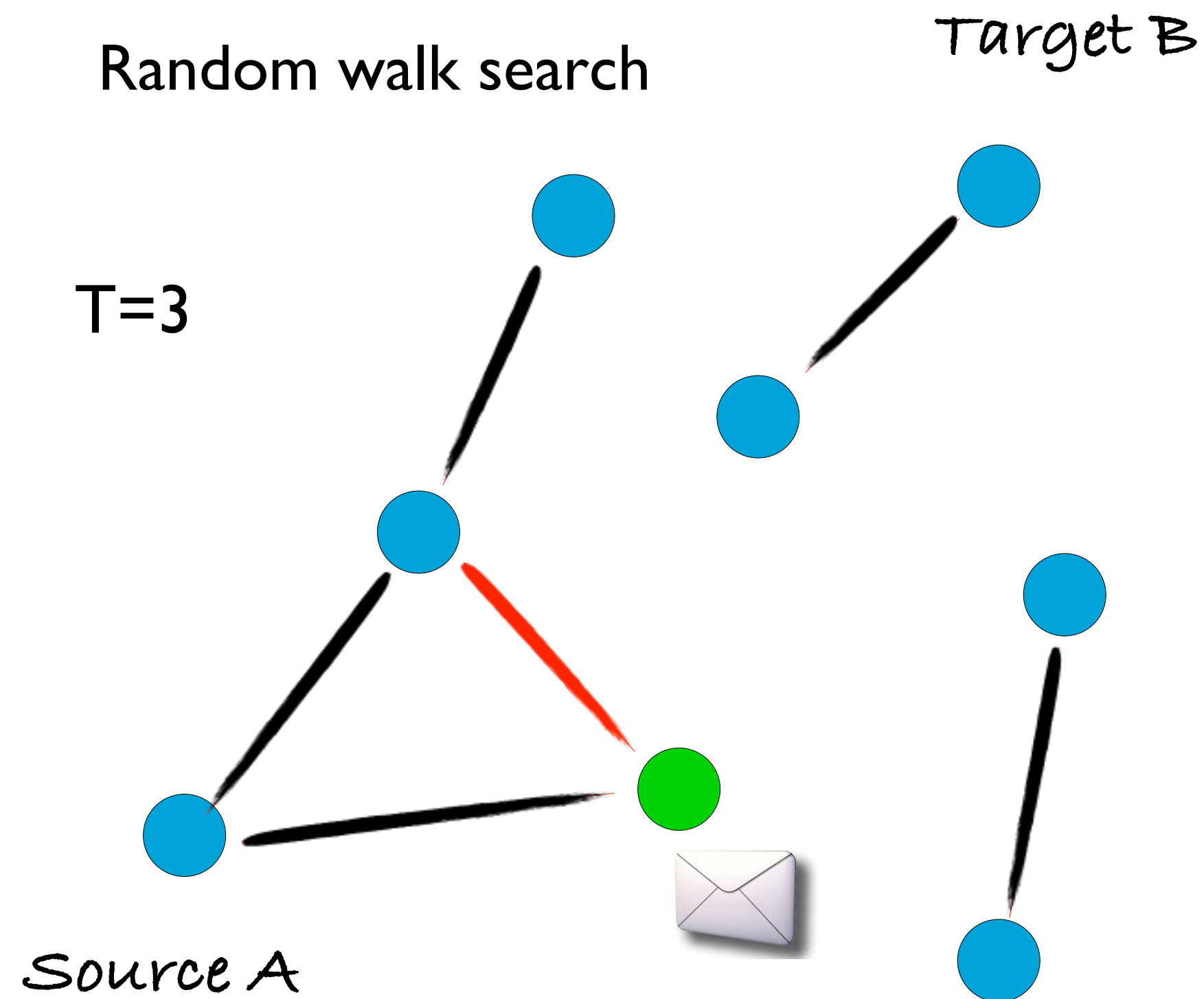
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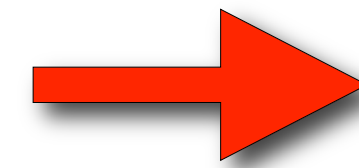
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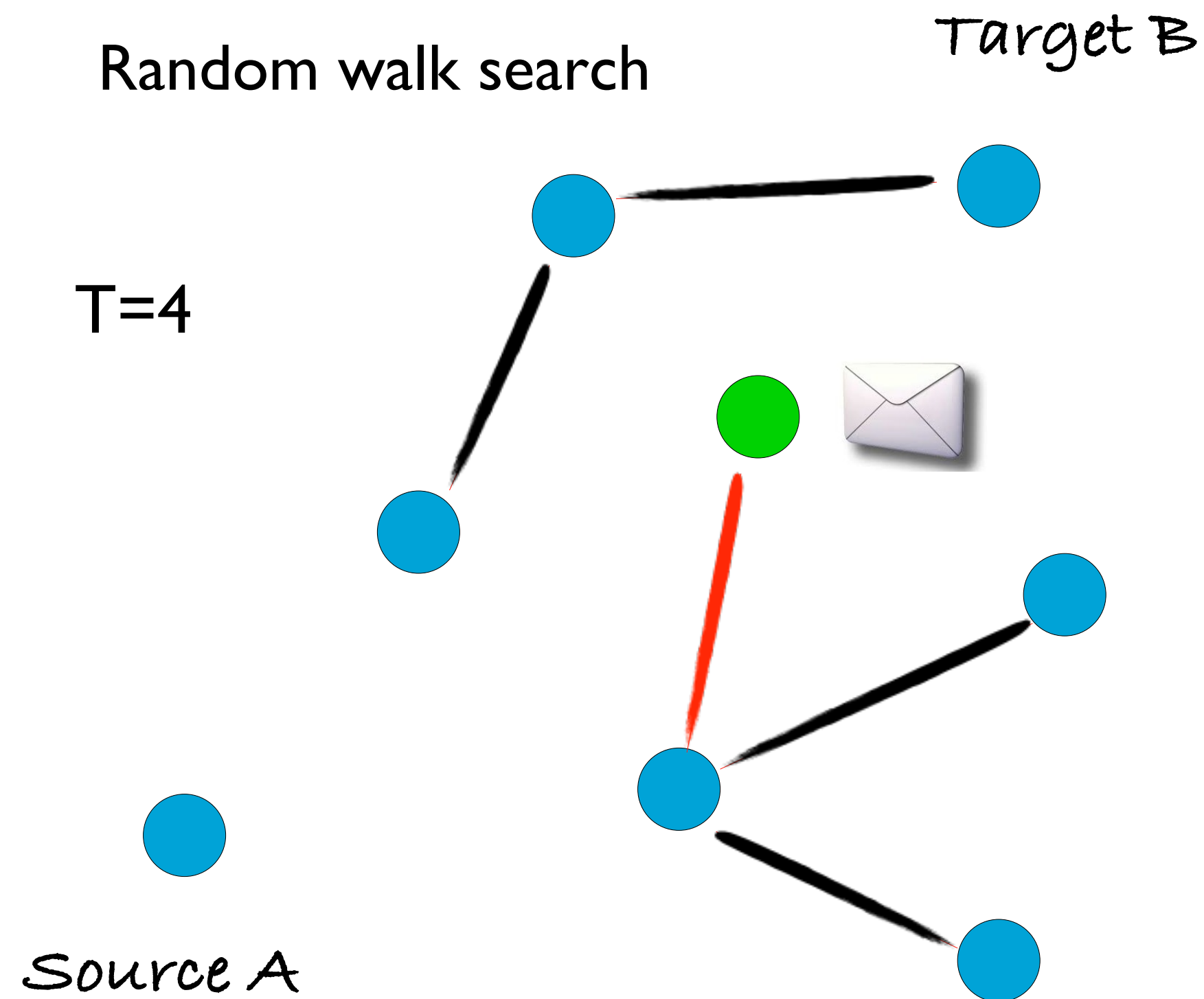
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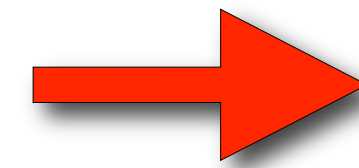
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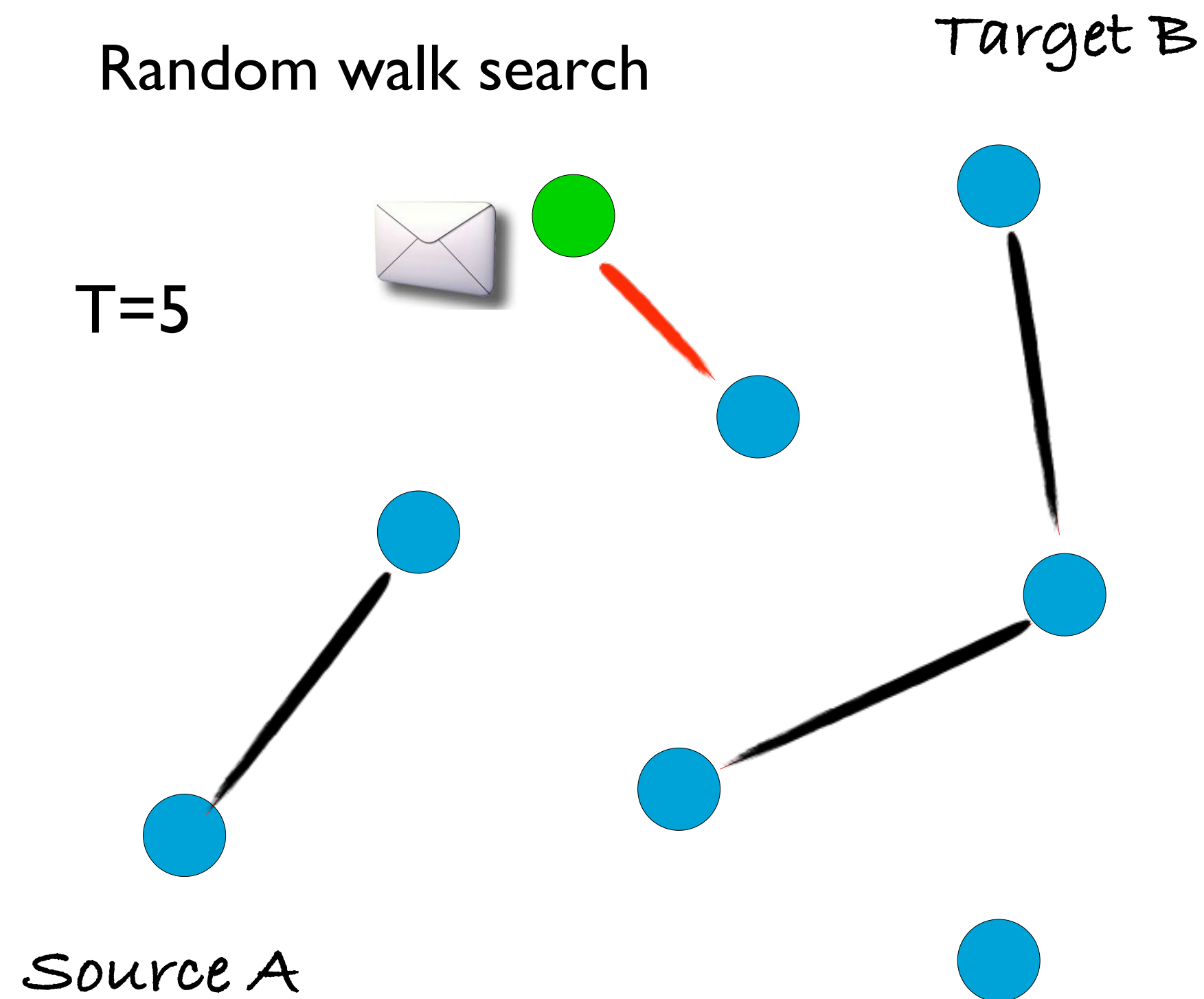
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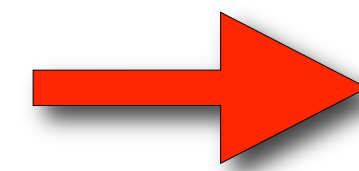
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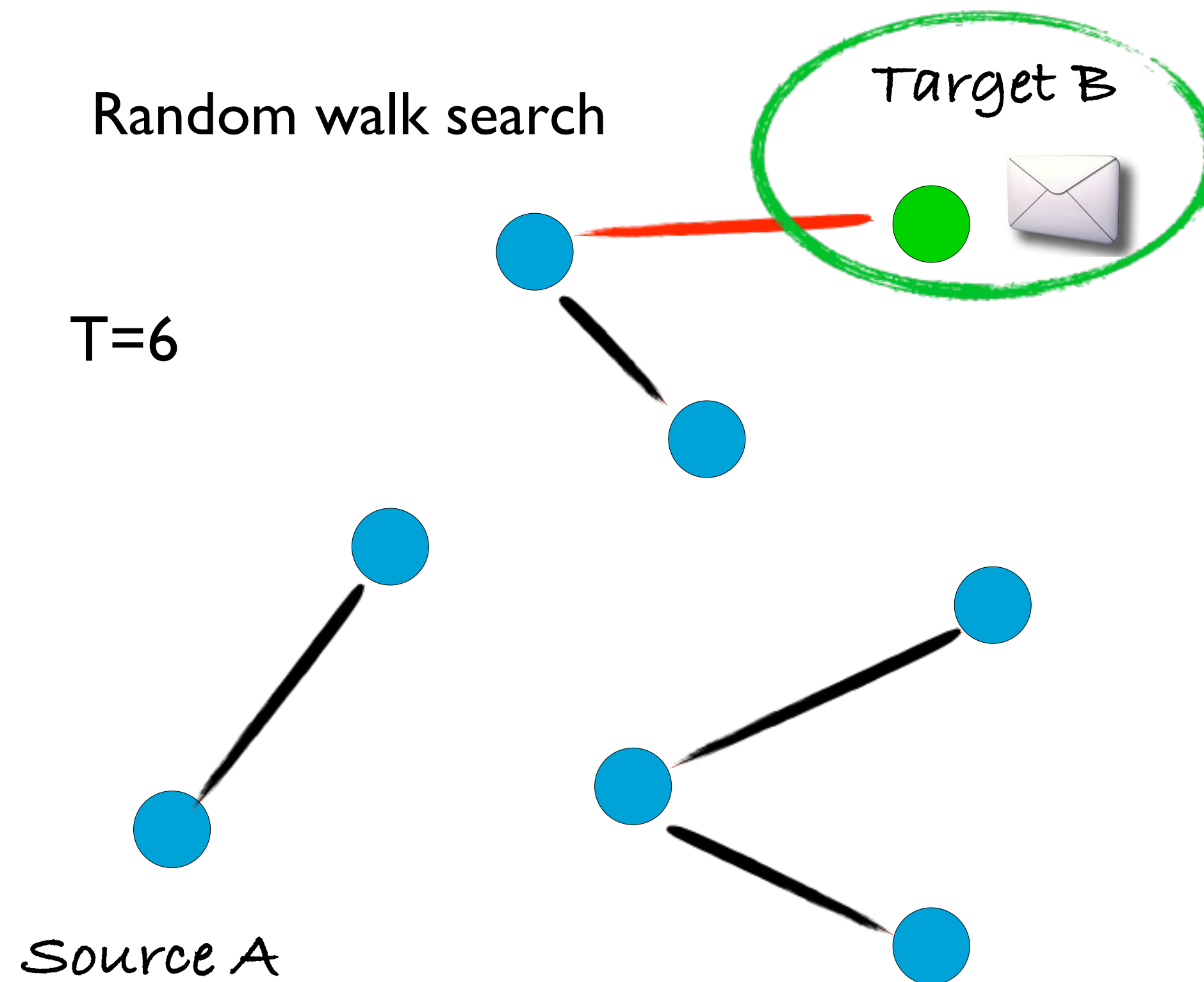
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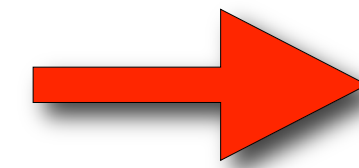
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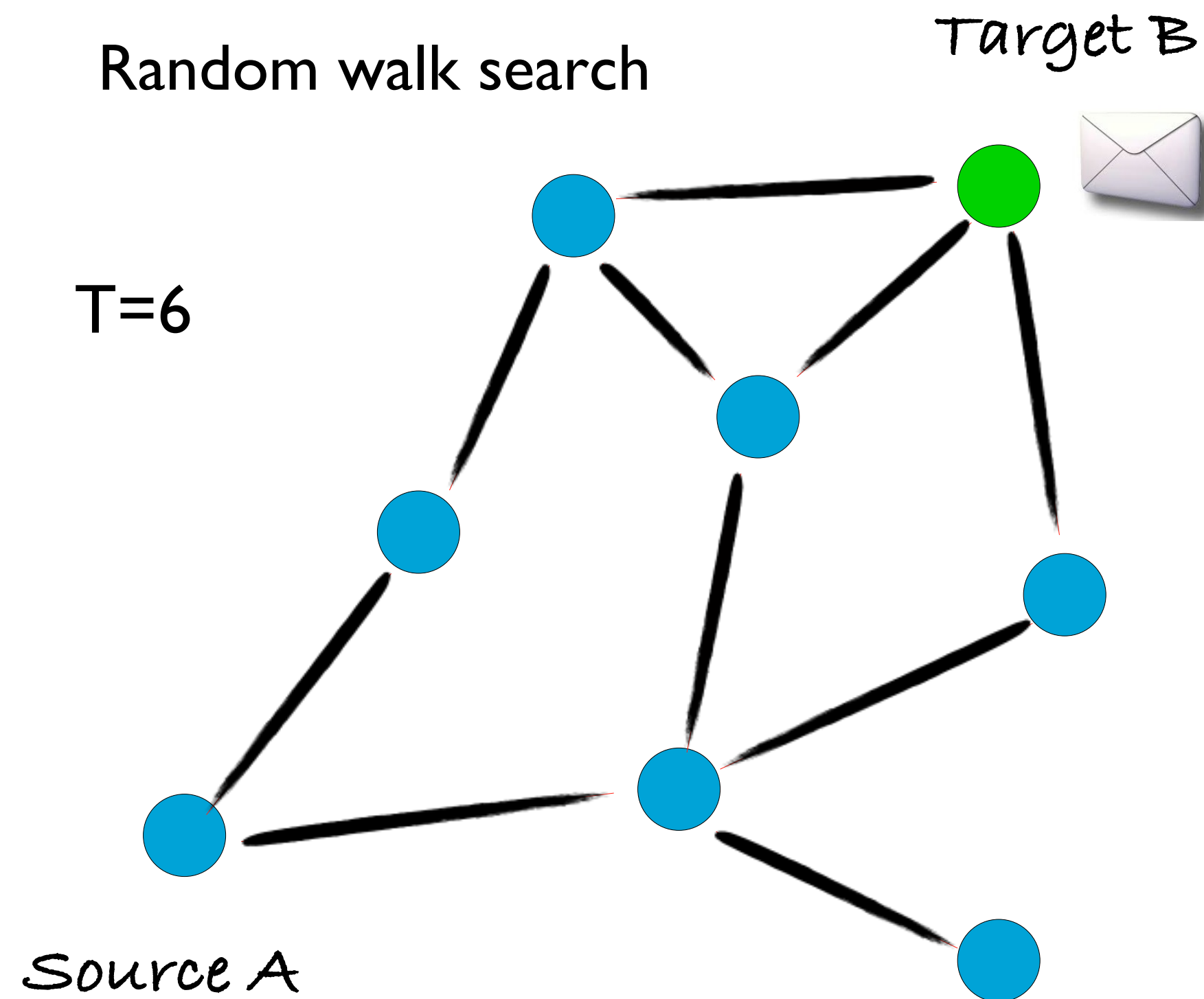
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Dynamical processes on temporal networks

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Time scales coupling



On a static network,
more links are available:
Very different process

Things to remember:

- Difference between dynamics ON and OF networks
- Definition of stochastic process on networks
- Examples of spreading phenomena, temporal networks
- How a stochastic process unfolds on temporal networks