

# Recommender Systems: Interaction-Based

### **Mining Massive Datasets**

Materials provided by Prof. Carlos Castillo — <u>https://chato.cl/teach</u> Instructor: Dr. Teodora Sandra Buda — <u>https://tbuda.github.io/</u>

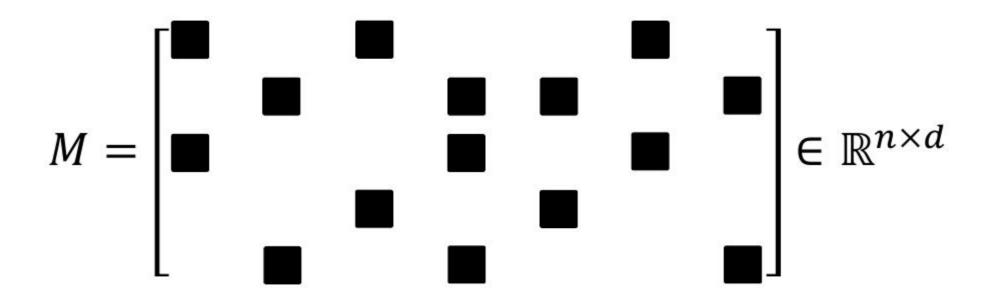
### Sources

- Data Mining, The Textbook (2015) by Charu Aggarwal (Section 18.5) – <u>slides by Lijun Zhang</u>
- Mining of Massive Datasets 2<sup>nd</sup> edition (2014) by Leskovec et al. (<u>Chapter 9</u>) - slides <u>A</u>, <u>B</u>

### Interaction-based recommendations

## Missing-value estimation/completion

. The matrix is extremely large and sparse



Only black squares have non-zero values.

# Types of algorithms

- Neighborhood-Based Methods
  - User-Based or Item-Based Similarity with Ratings
- Graph-Based Methods
- Clustering Methods
  - Adapting k-Means Clustering or Adapting Co-Clustering
- Latent Factor Models
  - Matrix Factorization, e.g., Singular Value Decomposition

### User-based similarity with ratings

- . Let  $\boldsymbol{I}_{\boldsymbol{u},\boldsymbol{v}}$  be common ratings between two users
- . Similarity: Pearson correlation coefficient

$$\operatorname{sim}(u,v) = \frac{\sum_{i \in I_{u,v}} (u_i - \hat{u}) \cdot (v_i - \hat{v})}{\sqrt{\sum_{i \in I_{u,v}} (u_i - \hat{u})^2 \cdot \sum_{i \in I_{u,v}} (v_i - \hat{v})^2}}$$
$$\hat{u} = \frac{1}{|u|} \sum_{i=1}^{|u|} u_i \quad \hat{v} = \frac{1}{|v|} \sum_{i=1}^{|v|} v_i \qquad \begin{array}{c} \operatorname{Note: averages are taken} \\ \operatorname{over all elements, not only} \\ \operatorname{ones in common} \end{array}$$

### User-based similarity with ratings (cont.) $\sum_{i=1}^{n} (y_i - \hat{y}) \cdot (y_i - \hat{y})$

$$\sin(u, v) = \frac{\sum_{i \in I_{u,v}} (u_i - u) \cdot (v_i - v)}{\sqrt{\sum_{i \in I_{u,v}} (u_i - \hat{u})^2 \cdot \sum_{i \in I_{u,v}} (v_i - \hat{v})^2}}$$

. Score of recommendation

$$\operatorname{score}(u,i) = \hat{u} + \frac{\sum_{v:v_i \neq \text{NULL}} \sin(v,u) \cdot (v_i - \hat{v})}{\sum_{v:I_{u,v} \neq \emptyset} |\sin(v,u)|}$$

Note: for efficiency one can take only the most similar users

### Exercise



$$\sin(u, v) = \frac{\sum_{i \in I_{u,v}} (u_i - \hat{u}) \cdot (v_i - \hat{v})}{\sqrt{\sum_{i \in I_{u,v}} (u_i - \hat{u})^2 \cdot \sum_{i \in I_{u,v}} (v_i - \hat{v})^2}}}{\sum_{i \in I_{u,v}} (v_i - \hat{v})}$$

$$\operatorname{score}(u,i) = \hat{u} + \frac{\sum_{v:v_i \neq \text{NULL}} \operatorname{SIM}(v,u) \cdot (v_i - v)}{\sum_{v:I_{u,v} \neq \emptyset} |\sin(v,u)|}$$

Complete yellow cells in spreadsheet:

- 1. Similarities *sim(u,v)*
- 2. Predicted rating of all movies that user *u* has not seen yet
- 3. Which movie is recommended?

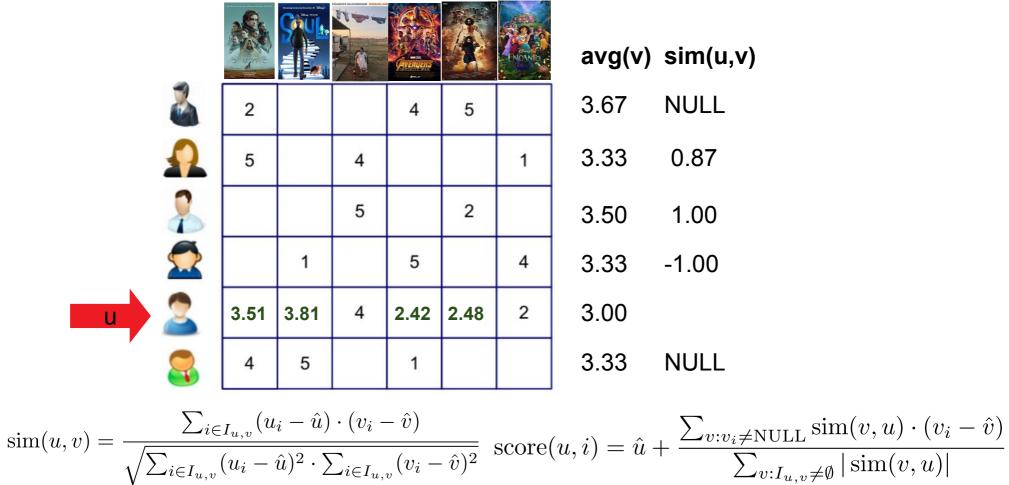


Spreadsheet link:

https://upfbarcelona.padlet.org/sandrabuda1/theory-exercises-tdmvfhddcnvfj5b8

Exercise from ML for Recommender Systems tutorial by Alex Karatzoglou, 2015.

#### Answer



Exercise from ML for Recommender Systems tutorial by Alex Karatzoglou. 2015.

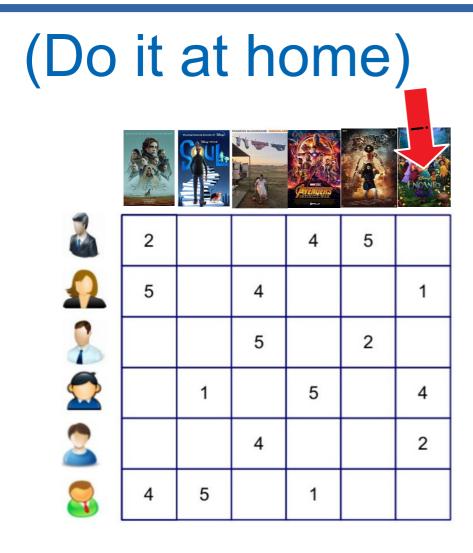
### You can do the same with items!

. Item-based similarities with ratings

$$\sin(i,j) = \frac{\sum_{u \in I_{i,j}} (u_i - \hat{i}) \cdot (u_j - \hat{j})}{\sqrt{\sum_{u \in I_{i,j}} (u_i - \hat{i})^2 \cdot \sum_{u \in I_{i,j}} (u_j - \hat{j})^2}}$$

. Item-based recommendations

$$\operatorname{score}(u,i) = \hat{i} + \frac{\sum_{j:u_j \neq \text{NULL}} \sin(i,j) \cdot (u_j - \hat{j})}{\sum_{j:I_{i,j} \neq \emptyset} |\sin(i,j)|}$$



- 1. Compute avg(j) for all items
- 2. Compute sim(i,j) for all items for which there is some intersection with i
- 3. Compute score(u,i) for all users who

have not seen i yet

$$\operatorname{sim}(i,j) = \frac{\sum_{u \in I_{i,j}} (u_i - \hat{i}) \cdot (u_j - \hat{j})}{\sqrt{\sum_{u \in I_{i,j}} (u_i - \hat{i})^2 \cdot \sum_{u \in I_{i,j}} (u_j - \hat{j})^2}}$$
$$\operatorname{score}(u,i) = \hat{i} + \frac{\sum_{j:u_j \neq \text{NULL}} \operatorname{sim}(i,j) \cdot (u_j - \hat{j})}{\sum_{j:I_{i,j} \neq \emptyset} |\operatorname{sim}(i,j)|}$$



$$2.33 + \frac{-1 \cdot (2 - 3.66) + 1 \cdot (4 - 3.33)}{|-1| + |-1| + |0.86| + |1|} = 2.94$$
  
$$2.33 + \frac{0.86 \cdot (5 - 4.33)}{|-1| + |-1| + |0.86| + |1|} = 2.48$$
  
$$2.33 + \frac{-1 \cdot (4 - 3.66) - 1 \cdot (5 - 3) + 1 \cdot (1 - 3.33)}{|-1| + |-1| + |0.86| + |1|} = 1.12$$

$$\sin(i,j) = \frac{\sum_{u \in I_{i,j}} (u_i - \hat{i}) \cdot (u_j - \hat{j})}{\sqrt{\sum_{u \in I_{i,j}} (u_i - \hat{i})^2 \cdot \sum_{u \in I_{i,j}} (u_j - \hat{j})^2}}$$

$$\operatorname{score}(u,i) = \hat{i} + \frac{\sum_{j:u_j \neq \text{NULL}} \operatorname{sim}(i,j) \cdot (u_j - \hat{j})}{\sum_{j:I_{i,j} \neq \emptyset} |\operatorname{sim}(i,j)|}$$

Exercise from ML for Recommender Systems tutorial by Alex Karatzoglou, 2015.

### Note

- . There are many ways of computing user-based similarity and item-based similarity
- . There are many ways of using these to generate recommendations
- . The method we have described is aware of the **bias of users**, in the sense of some users being more positive/negative than others in general

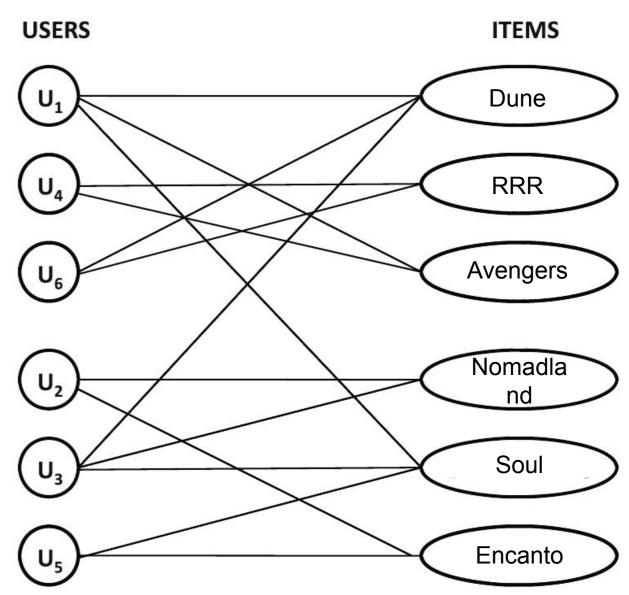
# Graph- and clustering-based methods

## Graph-based methods

- Bipartite user-item graph with nodes N<sub>u</sub> U N<sub>i</sub>
- . N<sub>u</sub> users
  - N<sub>u</sub> items

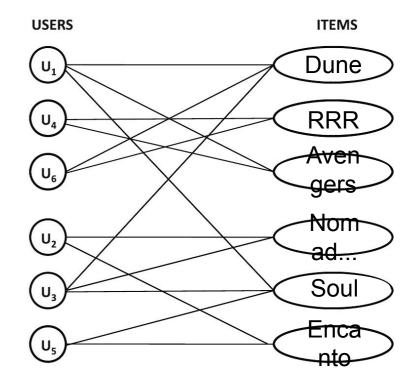
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. Non-zero utility  $\Rightarrow$  edge



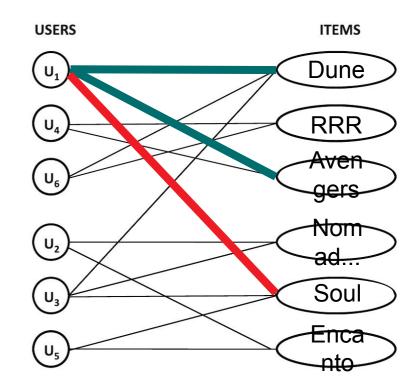
## Graph-based methods (cont.)

- . Use graph-based methods
  - Random walk with restart to a user or item
  - SimRank (not seen in class)
- . Low "random jump" probability might favor popular items



## Graph-based methods (cont.)

- . Signed networks can be used
  - Remember to interpret ratings with respect to user and item averages
  - Below average rating  $\Rightarrow$  -
  - Above average rating  $\Rightarrow$  +
- . Positive link prediction problem



### Clustering methods

### . Motivations

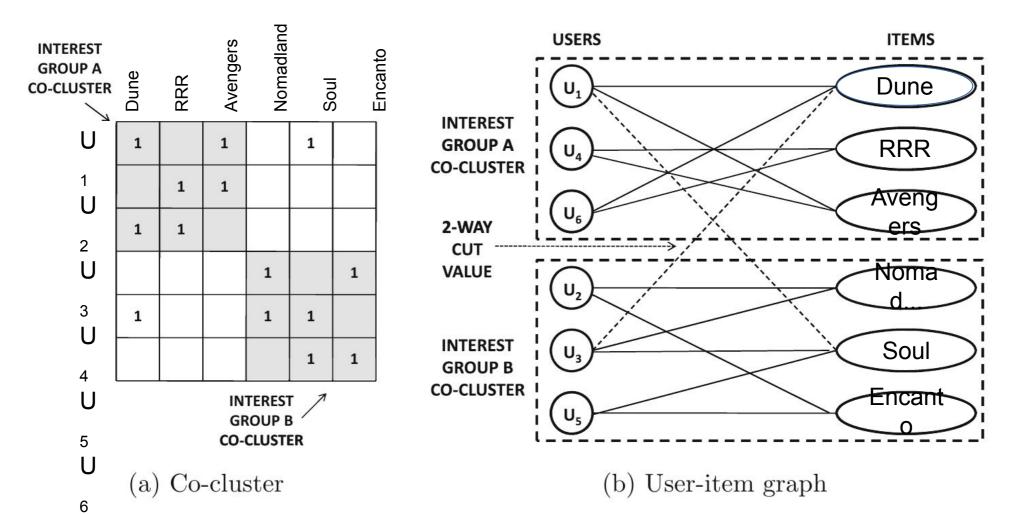
- Reduce computational cost
- To some extent address data sparsity
- . Results of clustering
  - Clusters of users for user-user similarity recs.
  - Clusters of items for item-item similarity recs.

## Clustering methods (cont.)

. User-user recommendation approach

- Cluster users into groups
- For any user u, compute average normalized rating for each item i the user has not seen
- Report these ratings for (u,i)
- Same with item-item recommendations
- . Neighborhoods will be smaller

### **Co-Clustering Approach**



### Summary

## Things to remember

- Interaction-based recommendations
  - User-based
  - Item-based
- Graph-based / clustering-based recommendations

### Exercises for TT16-TT18

- . Mining of Massive Datasets 2<sup>nd</sup> edition (2014) by Leskovec et al. Note that some exercises cover advanced concepts:
  - Exercises 9.2.8
  - Exercises 9.3.4
  - Exercises 9.4.6