

# Association Rules

## Mining Massive Datasets

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# Sources

- Data Mining, The Textbook (2015) by Charu Aggarwal (Chapters 4, 5) – [slides by Lijun Zhang](#)
- Mining of Massive Datasets 2<sup>nd</sup> edition (2014) by Leskovec et al. ([Chapter 6](#)) - [slides](#)
- Data Mining Concepts and Techniques, 3<sup>rd</sup> edition (2011) by Han et al. (Chapter 6)
- Introduction to Data Mining 2<sup>nd</sup> edition (2019) by Tan et al. (Chapters 5, 6) – [slides ch5](#), [slides ch6](#)

# What is a rule

- A rule is of the form  $X \Rightarrow Y$ 
  - $X$  and  $Y$  are itemsets
- $X$  is the antecedent,  $Y$  is the consequent
- The **confidence** of the rule is:

$$\text{conf}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X)}$$

# Confidence of a rule

- The **confidence** of the rule  $X \Rightarrow Y$  is:

$$\text{conf}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X)}$$

- This is the conditional probability of  $X \cup Y$  occurring in a transaction, given that  $X$  occurs in the transaction

# Confidence of a rule (cont.)

tid	Set of items
1	Bread, Jam, Juice
2	Tofu, Juice, Tomatoes
3	Bread, Strawberries, Tofu, Juice
4	Tofu, Juice, Tomatoes
5	Strawberries, Juice, Tomatoes

$\text{conf}(\{\text{tofu, juice}\} \Rightarrow \{\text{tomatoes}\}) = ?$

# Confidence of a rule (cont.)

tid	Set of items
1	Bread, Jam, Juice
2	Tofu, Juice, Tomatoes
3	Bread, Strawberries, Tofu, Juice
4	Tofu, Juice, Tomatoes
5	Strawberries, Juice, Tomatoes

$$\begin{aligned}\text{conf}(\{\text{tofu, juice}\} \Rightarrow \{\text{tomatoes}\}) &= \frac{\text{sup}(\{\text{tofu, juice, tomatoes}\})}{\text{sup}(\{\text{tofu, juice}\})} \\ &= \frac{0.4}{0.6} = \frac{2}{3}\end{aligned}$$

# X and Y are sets of items

$$\text{conf}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X)}$$

- The “union” in the above definition is confusing for some people, because conditional probability definitions use “intersection”
- Remember that that the set of transactions containing  $X \cup Y$  is the set of transactions containing  $X$  intersected with the set of transactions containing  $Y$
- The set of transactions containing “ $X \cap Y$ ” is **irrelevant** for the purposes of computing confidence, e.g., **in the previous exercise,  $\{\text{tofu, juice}\} \cap \{\text{tomato}\}$  is an empty set**

# Lift of a rule

- The **lift** of the rule  $X \Rightarrow Y$  is:

$$\text{lift}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X) \text{sup}(Y)}$$

- This is the ratio between the observed support and the expected support if  $X$  and  $Y$  were independent



# Exercise



$$\text{conf}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X)}$$

$$\text{lift}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X) \text{sup}(Y)}$$

Rule	Support $\text{sup}(X \cup Y)$	Confidence	Lift
$A \Rightarrow D$			
$C \Rightarrow A$			
$A \Rightarrow C$			
$B \& C \Rightarrow D$			

# Answers



$$\text{conf}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X)}$$

$$\text{lift}(X \Rightarrow Y) = \frac{\text{sup}(X \cup Y)}{\text{sup}(X) \text{sup}(Y)}$$

Rule	Support	Confidence	Lift
$A \Rightarrow D$	$2/5$	$2/3$	$10/9$
$C \Rightarrow A$	$2/5$	$2/4$	$5/6$
$A \Rightarrow C$	$2/5$	$2/3$	$5/6$
$B \& C \Rightarrow D$	$1/5$	$1/3$	$5/9$

# Association rule (minsup, minconf)

- Let  $X, Y$  be two itemsets; the rule  $X \Rightarrow Y$  is an **association rule** of minimum support **minsup** and minimum confidence **minconf** if:

$$\text{sup}(X \Rightarrow Y) \geq \text{minsup}$$

and

$$\text{conf}(X \Rightarrow Y) \geq \text{minconf}$$

# Summary

# Things to remember

- Association rule of minsup and minconf
- The concepts of **confidence** and **lift**

# Exercises for TT11-TT12

- Data Mining, The Textbook (2015) by Charu Aggarwal
  - Exercises 4.9 → 1-3, 5, 7-8
  - Exercises 5.7 → 1-5
- Mining of Massive Datasets 2<sup>nd</sup> edition (2014) by Leskovec et al.
  - Exercises 6.1.5 → 6.1.1-6.1.7
- Introduction to Data Mining 2<sup>nd</sup> edition (2019) by Tan et al.
  - Exercises 5.10 → 2-7